

For #1-6, simplify the following square roots. Leave your answer in simplest radical form. (No decimals)

1. $\sqrt{-48}$

$10 \sqrt{3} \quad 4i\sqrt{3}$

2. $-3\sqrt{-49}$

$-3 \cdot 7i$
 $-21i$

3. $-\sqrt{-175}$

$25 \sqrt{7}$
 $-5i\sqrt{7}$

4. $\frac{3}{2}\sqrt{-12}$

$\frac{3}{2} \cdot 2i\sqrt{3}$
 $3i\sqrt{3}$

5. $\sqrt{-224}$

$10 \sqrt{14}$
 $4i\sqrt{14}$

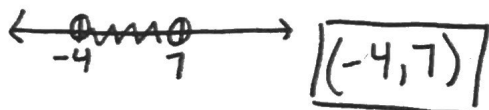
6. $-\frac{1}{4}\sqrt{-8}$

$-\frac{1}{4} \cdot 2i\sqrt{2}$
 $-\frac{1}{2}i\sqrt{2}$

For #7-9, solve the quadratic inequality and write the result in interval notation.

7. $x^2 - 3x - 4 < 24 \rightarrow -4 < 24 \checkmark$

$x^2 - 3x - 28 < 0$
 $(x-7)(x+4) < 0$
 $x=7$
 $x=-4$



8. $3x^2 - 21x \geq 0$

$3x(x-7) \geq 0$
 $x=0$
 $x=7$



$(-\infty, 0] \cup [7, \infty)$

9. $x^2 + 8x + 12 > 0$

$(x+6)(x+2) > 0$
 $x=-6$
 $x=-2$
 $(-\infty, -6) \cup (-2, \infty)$

10. $2x^2 + 12x + 10 \leq 0$

$(2x+10)(x+1) \leq 0$
 $x=-5$
 $x=-1$
 $[-5, -1]$

For #10-15, find the discriminant of the functions. Identify how many and what type of solutions. Then solve using the quadratic formula.

10. $x^2 - 4x + 5 = 0$

$(-4)^2 - 4(1)(5)$
 $16 - 20 = -4$
 $\frac{4 \pm \sqrt{-4}}{2}$
 $\frac{4 \pm 2i}{2} \rightarrow 2 \pm i$

11. $x^2 + 6x - 13 = 0$

$(6)^2 - 4(1)(-13)$
 $36 + 52 = 88$
 $\frac{-6 \pm \sqrt{88}}{2} \rightarrow \frac{-6 \pm 2\sqrt{11}}{2}$

Disc: -4
Type of Sol: 2 imag/comp.
Solutions: $2 \pm i$

Disc: 88
Type of Sol: 2 real sol.
Solutions: $-3 \pm \sqrt{11}$

$$12. x^2 + 6x + 5 = 0$$

$$(6)^2 - 4(1)(5)$$

$$36 - 20 = 16$$

$$\frac{-6 \pm \sqrt{16}}{2} \rightarrow \frac{-6 \pm 4}{2}$$

Disc: 16
 Type of Sol: 2 real sol.
 Solutions: $x = -1$ $x = -5$

$$14. x^2 - 5x + 8 = 0$$

$$(-5)^2 - 4(1)(8)$$

$$25 - 32 = -7$$

$$\frac{5 \pm i\sqrt{7}}{2}$$

Disc: -7
 Type of Sol: 2 imag/comp.
 Solutions: $\frac{5 \pm i\sqrt{7}}{2}$

For #16-27, solve using any method.

$$16. x^2 - 7x - 3 = 0$$

$$(-7)^2 - 4(1)(-3)$$

$$49 + 12 = 61$$

$$\boxed{\frac{7 \pm \sqrt{61}}{2}}$$

$$18. x^2 - 6x = 0$$

$$x(x-6) = 0$$

$$\boxed{x=0 \quad x=6}$$

$$13. x^2 + 4x + 2 = 0$$

$$(4)^2 - 4(1)(2)$$

$$16 - 8 = 8$$

$$\frac{-4 \pm \sqrt{8}}{2}$$

$$\frac{-4 \pm 2\sqrt{2}}{2}$$

Disc: 8
 Type of Sol: 2 real sol
 Solutions: $-2 \pm \sqrt{2}$

$$15. x^2 - 3x + 10 = 0$$

$$(-3)^2 - 4(1)(10)$$

$$9 - 40 = -31$$

$$\frac{3 \pm \sqrt{-31}}{2} \rightarrow \frac{3 \pm i\sqrt{31}}{2}$$

Disc: -31
 Type of Sol: 2 imag/comp.
 Solutions: $\frac{3 \pm i\sqrt{31}}{2}$

$$17. x^2 + 5x - 6 = 0$$

$$(x+6)(x-1)$$

$$\boxed{x = -6 \quad x = 1}$$

$$19. 2x^2 - 7x + 3 = 0$$

$$2x^2 - 6x - x + 3$$

$$2x(x-3) - 1(x-3)$$

$$(2x-1)(x-3)$$

$$\boxed{x = 1/2 \quad x = 3}$$

$$20. 3x^2 - 5x + 6 = -4$$

$$3x^2 - 5x + 10 = 0$$

$$(-5)^2 - 4(3)(10)$$

$$25 - 120 = -95$$

$$\frac{5 \pm \sqrt{-95}}{6} \rightarrow \boxed{\frac{5 \pm i\sqrt{95}}{6}}$$

$$21. x^2 + 11x = 3x - 10$$

$$x^2 + 8x + 10 = 0$$

$$(8)^2 - 4(1)(10)$$

$$64 - 40 = 24$$

$$\frac{-8 \pm \sqrt{24}}{2} \rightarrow \frac{-8 \pm 2\sqrt{6}}{2} \rightarrow \boxed{-4 \pm \sqrt{6}}$$

$$22. 14 - 3x^2 = 2x$$

$$3x^2 + 2x - 14$$

$$(2)^2 - 4(3)(-14)$$

$$4 + 168 \quad \frac{-2 \pm \sqrt{172}}{2 \cdot 3}$$

$$172$$

$$\frac{-2 \pm 2\sqrt{43}}{6} = \boxed{\frac{-1 \pm \sqrt{43}}{3}}$$

$$23. 7 - 8x^2 = 6x + 16$$

$$8x^2 + 6x + 9 = 0$$

$$6^2 - 4(8)(9) \quad \frac{-6 \pm \sqrt{-252}}{2 \cdot 8}$$

$$36 - 288$$

$$-252$$

$$\frac{-6 \pm 6i\sqrt{7}}{16} \rightarrow \boxed{\frac{-3 \pm 3i\sqrt{7}}{8}}$$

$$24. 5x^2 - 125 = 0$$

$$5x^2 = 125$$

$$x^2 = 25$$

$$\boxed{x = \pm 5}$$

$$25. 2(x+1)^2 - 3 = 7$$

$$2(x+1)^2 = 10$$

$$(x+1)^2 = 5$$

$$x+1 = \pm\sqrt{5}$$

$$\boxed{x = -1 \pm \sqrt{5}}$$

$$26. x^2 + 24x + 75 = -5$$

$$x^2 + 24x + 80 = 0$$

$$(x+20)(x+4)$$

$$\boxed{x = -20 \quad x = -4}$$

$$27. 3x^2 - 12x + 15 = -15$$

$$3x^2 - 12x + 30 = 0$$

$$\cancel{(-12)^2 - 4(3)(30)}$$

$$(-12)^2 - 4(3)(30)$$

$$144 - 360$$

$$-216$$

$$\frac{12 \pm \sqrt{-216}}{2 \cdot 3}$$

$$\frac{12 \pm 6i\sqrt{6}}{6}$$

$$\boxed{2 \pm i\sqrt{6}}$$